

Determine if the given points are ON, INSIDE, or OUTSIDE the given circle:

Center = $(5, -2)$

(SHOW ALL YOUR WORK)

Circle: $(x - 5)^2 + (y + 2)^2 = 36$

Radius = 6

1. $(10, 0)$

2. $(3, 1)$

3. $(-2, -2)$

$$r = \sqrt{(10-5)^2 + (0+2)^2}$$

$$5^2 + 2^2$$

$$25 + 4$$

$$\sqrt{29} = 5.4$$

inside

$$r = \sqrt{(5-3)^2 + (-2-1)^2}$$

$$2^2 + (-3)^2$$

$$4 + 9$$

$$\sqrt{13} = 3.4$$

inside

$$r = \sqrt{(-2-5)^2 + (-2+2)^2}$$

$$(-7)^2 + 0$$

$$\sqrt{49} = 7$$

Outside

4. A circle has a radius of 2 and a center of $(2, -3)$. Will the following points lie on the circle?

a. $(2, -5)$

b. $(3, -1)$

$$r = \sqrt{(2-2)^2 + (-3+5)^2}$$

$$0 + 2^2$$

$$\sqrt{4} = 2$$

on

$$r = \sqrt{(3-2)^2 + (-1+3)^2}$$

$$(1)^2 + (2)^2$$

$$1 + 4$$

$$\sqrt{5} = 2.2$$

Outside

5. Austin loves listening to his favorite country station, 101.5 Kicks fm. On a map, the station's headquarters are located at $(7, 3)$ and emits a signal that reaches a 50 mile radius.

a. Can Austin listen to his favorite station when he's chilling by the pool at a friend's house who lives at $(49, -5)$?

$$r = \sqrt{(49-7)^2 + (-5-3)^2}$$

$$(42)^2 + (-8)^2$$

$$1764 + 64$$

$$\sqrt{1828}$$

42.7 miles

Austin is inside the circle so he can get the signal

Convert

6. The Space Race in the 1960's between The Soviets and The Americans was a race to see who could get a spacecraft to the moon first. The moon has a 2-dimensional region of: $x^2 + y^2 + 882x - 166y + 90,345 = 0$.
Which country "won" the space race (landed on the moon)?

$$(x^2 + 882x \frac{194,481}{441.441})^2 + (y^2 - 166y + \frac{6889}{83.83}) = -90345 + 194,481 + 6889$$

$$(x + 441)^2 + (y - 83)^2 = 111,025$$

Russia shoots a rocket that lands at: $(-100, 80)$

Center = $(-441, 83)$
 $r = 333.2$

$$r = \sqrt{(-441 + 100)^2 + (83 - 80)^2}$$

$$= \sqrt{(-341)^2 + (3)^2}$$

$$= \sqrt{116281 + 9}$$

$$= \sqrt{116290}$$

$$r = 341.01$$

Russia
overshot
the moon

USA shoots a rocket that lands at: $(-400, -200)$

Center $(-441, 83)$
 $r = 333.2$

$$r = \sqrt{(-441 + 400)^2 + (83 + 200)^2}$$

$$= \sqrt{(41)^2 + (283)^2}$$

$$= \sqrt{1681 + 80089}$$

$$= \sqrt{81770}$$

$$r = 285.8$$

USA
Landed
on
the moon

7. Clowns are roaming around different areas of Acworth. One clown is at $x^2 + 6x + y^2 - 31 = 0$ And the other clown is roaming a center of $(-2, -2)$ with a radius of 4 miles. Will anyone be attacked by clowns?

$$(x^2 + 6x + \frac{9}{3.3})^2 + y^2 = 31 + 9$$

a. Your house is at $(6, 0) = 9$ miles outside

$$\text{Clown 1} = r = \sqrt{(6+3)^2 + (0+0)^2}$$

$$= \sqrt{(9)^2}$$

$$= 9$$

$$\text{Clown 2} = r = \sqrt{(6+2)^2 + (0-2)^2}$$

$$= \sqrt{8^2 + 4^2}$$

$$= \sqrt{64+16} = \sqrt{80}$$

b. Your friend's house is at $(3, -3)$

$$\text{Clown 1} = \sqrt{(3+3)^2 + (-3+0)^2}$$

$$= \sqrt{(9)^2 + (3)^2}$$

$$= \sqrt{81+9}$$

$$= \sqrt{90} = 9.5 \text{ miles}$$

$$\text{Clown 2} = \sqrt{(3+2)^2 + (-3+2)^2}$$

$$= \sqrt{(5)^2 + (-1)^2}$$

$$= \sqrt{25+1}$$

$$= \sqrt{26} = 5.1 \text{ miles}$$

You Both
are safe.

outside