

$$(x-h)^2 + (y-k)^2 = r^2$$

Finding the equation of the circle is important!

1. A circle has a radius of 2 and a center of (2, -3). Will the following points lie on the circle?

a. (2, -5)  
 $(2-2)^2 + (-5+3)^2 = 2^2$   
 $0 + 4 = 4$   
 $4 = 4$  yes!

b. (3, -1)  
 $(3-2)^2 + (-1+3)^2 = 2^2$   
 $(1)^2 + (2)^2 = 4$   
 $1 + 4 = 4$   
 $5 = 4$  Not on the circle outside O

2. Casey's dartboard is a circle centered at the origin with a radius of 8 inches. He throws 3 darts:

- a) The first dart hits (-3, 5)
- b) The second dart hits (4, 8)
- c) The third dart hits  $(2\sqrt{5}, 2\sqrt{11})$

$$(x-h)^2 + (y-k)^2 = r^2$$

$$(x-0)^2 + (y-0)^2 = 64$$

Are his darts inside, outside, or on the board?

a)  $(-3-0)^2 + (5-0)^2 = 64$   
 $(-3)^2 + (5)^2 = 64$   
 $9 + 25 = 64$   
 $34 = 64$   
 (inside)

b)  $(4-0)^2 + (8-0)^2 = 64$   
 $(4)^2 + (8)^2 = 64$   
 $16 + 64 = 64$   
 $80 = 64$   
 (outside)

c)  $(2\sqrt{5}-0)^2 + (2\sqrt{11}-0)^2 = 64$   
 $(2\sqrt{5})^2 + (2\sqrt{11})^2 = 64$   
 $4 \cdot 5 + 4 \cdot 11 = 64$   
 $20 + 44 = 64$   
 $64 = 64$   
 (on)

3. The new Georgia Dome is being built in the region w/ equation:

$$x^2 + y^2 - 6x + 20y - 39,891 = 0$$

$$x^2 - 6x + \frac{9}{4} + y^2 + 20y + \frac{100}{4} = 39,891 + \frac{9}{4} + \frac{100}{4}$$

Several churches in the area are protesting that the church might interfere with their building:

Mount Vernon Baptist is located at: (100, 105)

$$(x-3)^2 + (y+10)^2 = 40,000$$

Friendship Baptist Church is located at: (-174, -58)

(a) If the churches lie within the area of the new stadium, what should the Falcons do?

(b) How much would be a fair price?  
 (opinion)

MVB:  $(100-3)^2 + (105+10)^2 = 40,000$   
 $22,634 = 40,000$

FBC:  $(-174-3)^2 + (-58+10)^2 = 40,000$   
 $33,633 = 40,000$

They are Both inside the area

4. The Space Race in the 1960's between The Soviets and The Americans was a race to see who could get a spacecraft to the moon first. The moon has a 2-dimensional region of:

$$x^2 + y^2 + 882x - 166y + 90,345 = 0$$

$$x^2 + 882x + \frac{194,481}{4} + y^2 - 166y + \frac{6889}{4} = -90,345 + \frac{194,481}{4} + \frac{6889}{4}$$

$$(x+441)^2 + (y-83)^2 = 111,025$$

Russia shoots a rocket that lands at: (-100, 80)

USA shoots a rocket that lands at: (-400, -200)

Which country "won" the space race (landed on the moon)?

Russia:  $(-100+441)^2 + (80-83)^2 = 111,025$

USA:  $(-400+441)^2 + (-200-83)^2 = 111,025$

larger means outside the area of moon → 116,290 = 111,025  
 one shoots

small is inside the area for moon → 81,770 = 111,025  
 lands on the Moon



5. A furniture store (at the origin) advertises free delivery within a 50 mile radius from the store. If a customer lives 28 miles east and 41 miles north of the store, does the customer qualify for free delivery?

(28, 41) Center

Radius

$$(x-28)^2 + (y-41)^2 = 50^2 = 2500$$

(a) What if they lived 30 miles west and 41 miles south?

$$(-30, -41)$$

x    y

$$(-30-28)^2 + (-41-41)^2 = 2500$$

$$3364 + 6724 = 2500$$

$$10,088 = 2500 \text{ outside the area!}$$

(b) What about 50 miles west?

$$(-50, 0) \quad (-50-28)^2 + (0-41)^2 = 2500$$

$$6084 + 1681 = 2500$$

$$7765 = 2500$$

nope - outside of area!

6. Clowns are roaming around different areas of Acworth. One clown is at  $x^2 + 6x + y^2 - 31 = 0$

And the other clown is roaming a center of  $(-2, -2)$  with a radius of 4 miles.

$$x^2 + 6x + 9 + y^2 = 31 + 9$$

$$(x+3)^2 + y^2 = 40 \quad C1$$

$$C2 \Rightarrow (x+2)^2 + (y+2)^2 = 16$$

Your house is at (6, 0)

Your friends house is at (3, -3)

Coach Harrison's house is at (2.3, 4.1)

$$C1 \quad (6+3)^2 + (0)^2 = 40$$

$$81 = 40 \text{ outside}$$

$$C1 \quad (3+3)^2 + (-3)^2 = 40$$

$$36 + 9 = 45 = 40 \text{ outside}$$

$$C1 \quad (2.3+3)^2 + (4.1)^2 = 40$$

$$28.09 + 16.81 = 44.9 = 40 \text{ outside}$$

$$C2 \quad (6+2)^2 + (0+2)^2 = 16 \text{ outside}$$

$$64 + 4 = 68 = 16$$

$$C2 \quad (3+2)^2 + (-3+2)^2 = 16$$

$$25 + 1 = 26 = 16 \text{ outside}$$

$$C2 \quad (2.3+2)^2 + (4.1+2)^2 = 16$$

$$18.49 + 37.21 = 55.7 = 16 \text{ outside}$$

Will anyone be attacked by clowns?

Your House is safe from Clowns! 😊

Your Friends House is safe from Clowns! 😊

Coach Harrison is Safe! 😊