

Parallel and Perpendicular Lines

Determine if the following equations are parallel, perpendicular, or neither.

1. $y = \frac{1}{2}x + 4$ $y = \frac{1}{2}x - 5$ $m_1 = \frac{1}{2}$ $m_2 = \frac{1}{2}$ Parallel	2. $3x + y = 5$ $m_1 = -3$ $x - 3y = -3$ $m_2 = \frac{1}{3}$ a) $3x + y = 5$ $y = -3x + 5$ Perp. b) $x - 3y = -3$ $\frac{-3y}{-3} = \frac{-x - 3}{-3}$ $y = \frac{1}{3}x + 1$	3. $y = \frac{1}{4}x + 3$ $m = \frac{1}{4}$ $2x + 8y = -8$ $m = -\frac{1}{4}$ $\frac{8y}{8} = \frac{-2x - 8}{8}$ $y = -\frac{1}{4}x - 1$ neither	4. $2x + 4y = 8$ $m = -\frac{1}{2}$ $3x + 6y = -6$ $m = -\frac{1}{2}$ a) $\frac{4y}{4} = -\frac{2x + 8}{4}$ $y = -\frac{1}{2}x + 2$ b) $\frac{6y}{6} = \frac{-3x - 6}{6}$ $y = -\frac{1}{2}x - 1$ Parallel
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Write the equation of a line parallel and a line perpendicular to the given equation.

Line	Parallel Lines	Perpendicular Lines
5. $y = \frac{1}{3}x + 1$ $(-3, 4)$ $M = \frac{1}{3}$	$m_{ } = \frac{1}{3}$ $(-3, 4)$ $4 = \frac{1}{3}(-3) + b$ $4 = -1 + b$ $5 = b$ $y = \frac{1}{3}x + 5$	$m_{\perp} = -3$ $(-3, 4)$ $4 = -3(-3) + b$ $4 = 9 + b$ $-9 = -9$ $-5 = b$ $y = -3x - 5$
6. $y = 4x + 2$ $(-8, -3)$ $M = 4$	$m_{ } = 4$ $(-8, -3)$ $-3 = 4(-8) + b$ $-3 = -32 + b$ $29 = b$ $y = 4x + 29$	$m_{\perp} = -\frac{1}{4}$ $(-8, -3)$ $-3 = -\frac{1}{4}(-8) + b$ $-3 = 2 + b$ $-2 = -2$ $-5 = b$ $y = -\frac{1}{4}x - 5$
7. $6x - 3y = 12$ $(-6, 1)$ $\frac{-3y}{-3} = \frac{-6x + 12}{-3}$ $y = 2x - 4$ $m = 2$	$m_{ } = 2$ $(-6, 1)$ $1 = 2(-6) + b$ $1 = -12 + b$ $+12 + 12$ $13 = b$ $y = 2x + 13$	$m_{\perp} = -\frac{1}{2}$ $(-6, 1)$ $1 = -\frac{1}{2}(-6) + b$ $1 = 3 + b$ $-3 = -3$ $-2 = b$ $y = -\frac{1}{2}x - 2$
8. $10x + 5y = 15$ $(-2, 0)$ $\frac{5y}{5} = \frac{-10x + 15}{5}$ $y = -2x + 3$	$m_{ } = -2$ $(-2, 0)$ $0 = -2(-2) + b$ $0 = 4 + b$ $-4 = b$ $y = -2x - 4$	$m_{\perp} = \frac{1}{2}$ $(-2, 0)$ $0 = \frac{1}{2}(-2) + b$ $0 = -1 + b$ $1 = b$ $y = \frac{1}{2}x + 1$